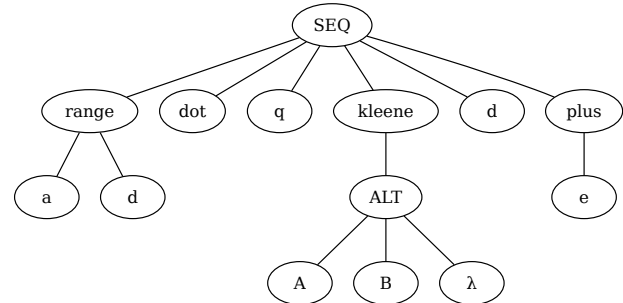


1. Similar to our discussion today in lecture, the regular expression $a \cdot d \cdot q(A|B|) \cdot de^+$ from the LL(1) grammar below would yield the “raw” or concrete parse tree on page 6.

| # | Rules |
|----|--|
| 1 | $RE \rightarrow ALT \$$ |
| 2 | $ALT \rightarrow SEQ ALT LIST$ |
| 3 | $ALT LIST \rightarrow pipe SEQ ALT LIST$ |
| 4 | $ALT LIST \rightarrow \lambda$ |
| 5 | $SEQ \rightarrow ATOM SEQ LIST$ |
| 6 | $SEQ \rightarrow \lambda$ |
| 7 | $SEQ LIST \rightarrow ATOM SEQ LIST$ |
| 8 | $SEQ LIST \rightarrow \lambda$ |
| 9 | $ATOM \rightarrow NUCLEUS ATOM MOD$ |
| 10 | $ATOM MOD \rightarrow kleene$ |
| 11 | $ATOM MOD \rightarrow plus$ |
| 12 | $ATOM MOD \rightarrow \lambda$ |
| 13 | $NUCLEUS \rightarrow open ALT close$ |
| 14 | $NUCLEUS \rightarrow char CHARRNG$ |
| 15 | $NUCLEUS \rightarrow dot$ |
| 16 | $CHARRNG \rightarrow dash char$ |
| 17 | $CHARRNG \rightarrow \lambda$ |

During the parse several steps can be performed to simplify the structure of the tree, resulting in:



In lecture ([show_re-sdt.pdf](#)) we discussed the **syntax directed translation** procedures that would be executed on a subset of the grammar rules. This question asks you to compose the pseudo code for the remaining production rules that didn't have their logic presented in lecture.

For guidance, you can use this visualization of [the parsing steps](#) for this question's example.

If you missed lecture, there is a lengthy explanation of the mechanics of **syntax directed translation** on page 4.

2. We presume your group has by now at least one working LL(1) parser from [l11-parsing.pdf](#). Take any of the many simple grammars we've had in lecture up until now (or one of your own design) and use it to develop a framework in the code base for attaching **SDT procedures** to particular production rules and have them executed (as shown in lecture) when end-of-production markers are encountered in the LL(1) parsing stack.

Develop for your group a working example that demonstrates at least following:

- Flip flops or rotates grammar symbols of a particular production rule's RHS.
For instance, the grammar rule is $A \rightarrow xYz$, but the AST children of A are in the order Yzx or zxY or zYx .
- "Flattens" a recursive rule (such as what happens to *SEQLIST* in the lecture example).
So grammar rules $B \rightarrow gB$ and $B \rightarrow g$ yield an AST node B with many g children, instead of most¹ B nodes having two children g and B .

Keep in mind, there is no practical use of option (a) above in the parsing of languages, it is simply a useful manipulation that is easy to code and verify in your implementation.

3. Same as question 2 **iff** your group has *two different code implementations*. Otherwise, you can ignore this question.

¹...all but the recursion terminating substitution.

4. Suppose you are given a correct, un-conflicted SLR(1) table and told the grammar it is for contains only one non-terminal. Can you deduce the grammar rules from this information? How? Or why not?

Hint: properly written grammars have a starting goal with \$ at the end of all its production rules, and therefore starting goals cannot have recursive rules.

Hint: here is an SLR(1) table for you two contemplate while you reason out your answer.

| | <i>a</i> | <i>c</i> | <i>q</i> | <i>x</i> | \$ |
|----|----------|----------|----------|----------|-------|
| 0 | | sh-1 | sh-2 | sh-3 | |
| 1 | | sh-4 | | sh-5 | |
| 2 | | | sh-6 | | |
| 3 | sh-7 | sh-8 | | | |
| 4 | sh-9 | | | | |
| 5 | | | | sh-10 | |
| 6 | | | sh-11 | | |
| 7 | | sh-12 | | | |
| 8 | sh-13 | | | | |
| 9 | | | | | sh-14 |
| 10 | | | | | sh-15 |
| 11 | | | | | sh-16 |
| 12 | | | | | sh-17 |
| 13 | | | | | sh-18 |
| 14 | Reduce 3 | | | | |
| 15 | Reduce 4 | | | | |
| 16 | Reduce 5 | | | | |
| 17 | Reduce 1 | | | | |
| 18 | Reduce 2 | | | | |

5. Construct a scanning function for our regular expression language on page 1 and reproduced below for your convenience.² It should generate output as sequences of pairwise tuples (not surprisingly very similar to the token output of the LUTHOR programming project). From a regular expression such as

Ab(cd-e+)*(.|012)3

your scanning logic should generate the **token stream** below:

```

RE  → ALT $
ALT → SEQ ALTLIST
ALTLIST → pipe SEQ ALTLIST
      | λ
SEQ     → ATOM SEQLIST
      | λ
SEQLIST → ATOM SEQLIST
      | λ
ATOM    → NUCLEUS ATOMMOD
ATOMMOD → kleene
      | plus
      | λ
NUCLEUS → open ALT close
      | char CHARRNG
      | dot
CHARRNG → dash char
      | λ

```

```

char A
char b
open (
char c
char d
dash -
char e
plus +
close )
kleene *
open (
dot .
pipe |
char 0
char 1
char 2
close )
char 3

```

```

char (
char p
char a
char r
char e
char n
open (
char t
char h
char e
char t
char i
char c
char a
char l
pipe |
close )
char -
char a
char l
char l
char y
char )
char x20
char c
char o
char r
char r
char e
char c
char t
char !
char x0a

```

Recall that a scanner generates only the terminals of a language — it will never output a *NUCLEUS*, these are formed by the parser when recognizing patterns in the terminals.

We need to be able to write regular expressions with the *char* data of asterisk (*), so we must have a method for **escaping** the special symbols of our RE language. We'll use the ubiquitous backslash (0x5c) for this purpose. It will be helpful to have a few other specially escaped characters as well, here is the full list:

| RE sequence | token stream | RE sequence | token stream |
|-------------|-----------------|-------------|-----------------|
| \\ | <i>char</i> \ | * | <i>char</i> * |
| \\+ | <i>char</i> + | \\. | <i>char</i> . |
| \\(| <i>char</i> (| \\) | <i>char</i>) |
| \\- | <i>char</i> - | \\s | <i>char</i> x20 |
| \\n | <i>char</i> x0a | \\ | <i>char</i> \ |

When turning a regular expression into a token stream, these backslash forms should emit a simple *char* terminal. For example, in the margin at the right is the expected output from a more complex regular expression:

\\(paren(thetical|)\\-ally\\)\\scorrect!\\n

Now here's the (small) kicker: Don't implement any of the scanning logic using your language's built-in regex features! We want to finish the course having **bootstrapped** our own REs and Lexer. We can't say that if you use *a regular expression library* from another source. In truth this requirement is not difficult to meet,³ none of the sequences above require looking ahead more than two characters at a time.

²This logic is referred to in WRECK as the "silly lexer," because it is quite barely a lexer.

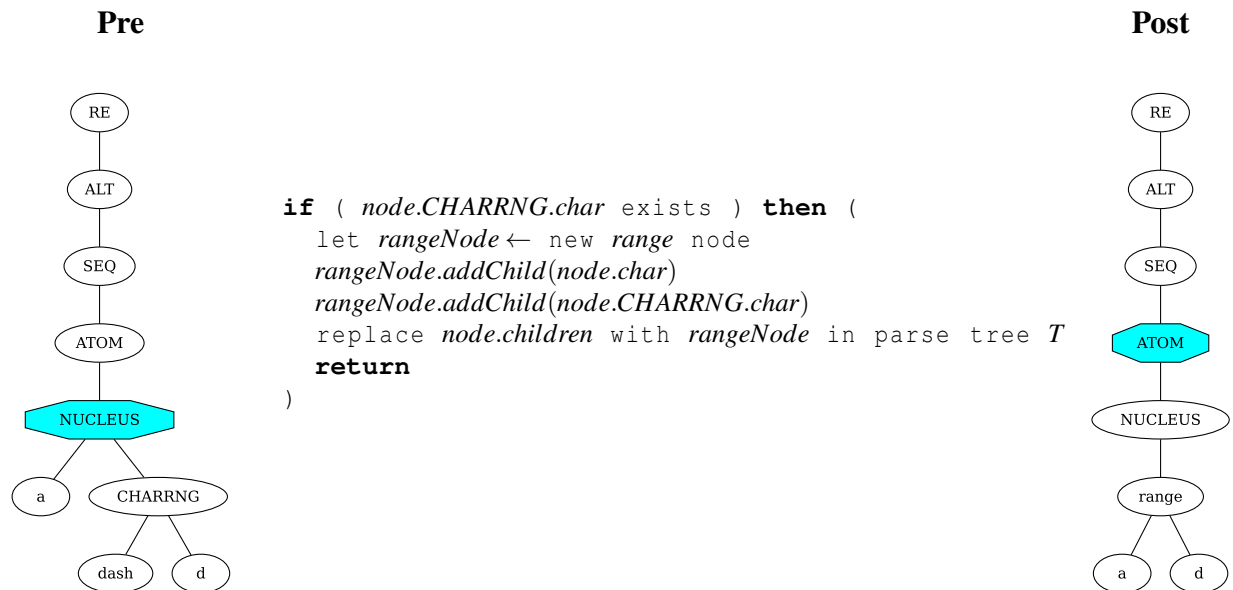
³A loop and one state variable?

Syntax Directed Translation (SDT) in brief

The thought exercise for question 1 has you determine the algorithms for massaging the raw parse tree (on page 6, also called a *concrete syntax tree*) into the simplified tree above.

Envision an algorithm where a **rule or non-terminal specific** function is invoked when each internal (non-terminal) node of a parse tree is completed. In this case *completed* means that no more children will be added to the node **and** no more children will be added to any descendants of the node. In the case of the LL parsing algorithm, this is everytime a production marker (*) is popped off the stack. See [show-re-sdt.pdf](#) and [the parsing steps](#) for a visual of the parsing algorithm.

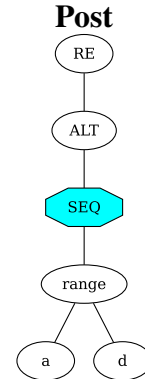
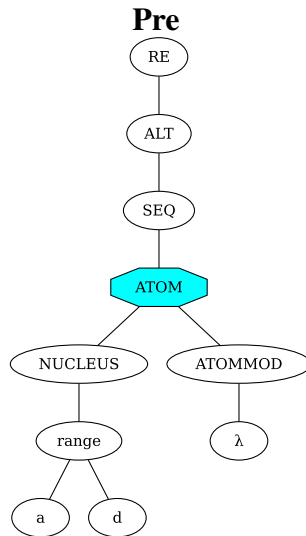
By way of example, consider how the first *NUCLEUS* node in the left-most derivation of $a-d.q(A|B|)*de+$ might be simplified immediately after the first application of rule 14 is completed. The regular expression part is $a-d$, which from the grammar above yields the partial⁴ parse tree with the *NUCLEUS* node at the left:



The pseudo code in the middle shows how the parse tree *NUCLEUS* node can be immediately simplified, with the resulting parse tree **Post** to the right. Some points for clarification:

- i. **Not all non-terminal nodes require simplification functions** — truly one skill to be developed here is choosing the nodes for simplification in order to *easily* arrive at a simplified parse tree.
- ii. The psuedo code uses terms directly from the grammar and the (partial) raw parse tree. How was the “path” of *node.CHARRNG.char* chosen in the logic? Because *node* \equiv *NUCLEUS* and *node.CHARRNG.char* is the most **convenient and unambiguous** identifier for the second child of *node*’s second child.
- iii. The node type of **range** is not a grammar symbol, but that’s OK — the input so far has been syntax verified, so we don’t need to maintain the originally parsed structure of the input.
- iv. Since we consider this simplification occurring as soon as a non-terminal node is *completed*, the tree does not yet show the *ATOMMOD* node deriving to λ and being appended as the right most child of the *ATOM* node now containing **range**.
- v. We can envision the **next simplification function** called will be the one for *ATOM* after production rule 9 is completed. The partial parse tree at that time is shown on the following page; since there is no + or * operator applied to **range** the *ATOM* can be “simplified away” leaving **range** as the first child of *SEQ*.

⁴It is a **partial** parse tree because it is still being constructed by an LL (top-down) parse — the only place you see full, raw parse trees are in university compilers courses — in practice simplification of the parse tree occurs hand-in-hand and concurrently with the parse!



Your task for question(s) 1 of this LGA: design the required simplification logic for transforming the (partial) LL(1) generated parse trees created during the recursive descent parse into a simplified AST (the tree on on page 1).

For completeness, we show the complete pseudo code for simplifying *NUCLEUS* nodes (grammar rules 13–15):

```

procedure NUCLEUS( node, parse tree T )

  if ( node.children[0] is open ) then (
    replace node with node.children[1] in parse tree T
    return
  )

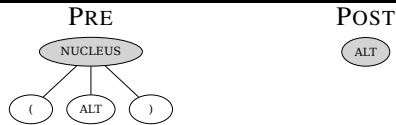
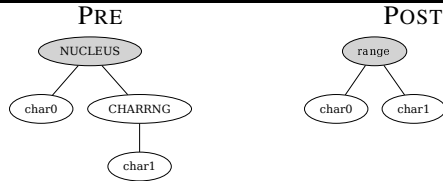
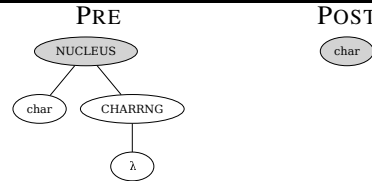
  if ( node.CHARRNG.char exists ) then (
    let rangeNode ← new range node
    rangeNode.addChild(node.char)
    rangeNode.addChild(node.CHARRNG.char)
    replace node.children with rangeNode in parse tree T
    return
  )

  if ( node.CHARRNG.child is λ ) then (
    remove node.CHARRNG child
    return
  )

  if ( node.child is dot ) then (
    replace node with node.child in parse tree T
    return
  )

```

Beginning on the following page are the transformations of the parse (sub)trees that occur depending on the production rule being processed. In all PRE trees, the grey node represents *node* of the *NUCLEUS* logic; in the POST **the only colored node** represents the **the same location in the parse tree** as the PRE grey *node*.

Rule 13, $NUCLEUS \rightarrow open\ ALT\ close$ **Rule 15**, $NUCLEUS \rightarrow dot$ **Rule 14** when $CHARRNG.char$ exists**Rule 14** when $CHARRNG.child$ is λ **“Raw” Parse Tree for input $a-d.q(A|B|)^*de+$, also called a *concrete parse tree***