

Construct a regular expression to match the following...

1. All bit patterns (0s and 1s) of a 32 bit integer,
2. All 32b integer bit patterns **without** two sequential identically valued bits,
3. Bit representations of arbitrarily large integers conforming to the pattern

$$\underbrace{000\dots0}_{n \text{ times}} \underbrace{111\dots1}_{n \text{ times}}$$

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$$(0|1)^{32}$$

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NOT $(01|10)^{16}$ WHICH PERMITS 0110...

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???

Limitations of Regular Languages

Regular languages cannot express arbitrarily deep recursive (nested) structures.

Examples:

- ▶ Cannot confirm matching parenthesis of mathematical expressions,
- ▶ Cannot confirm matching parenthesis of conventional compositional syntax of function calls $(\log(\sin(3)))$,
- ▶ Cannot confirm matching curly braces of compound statements in C, C++, Java, Javascript, ...
- ▶ And the simplest example: $0^n 1^n$

For this very reasonable language feature, we need a higher level of language definitions: **context free grammars**.